# Backbone Dynamics of the c-Jun Leucine Zipper: <sup>15</sup>N NMR Relaxation Studies<sup>†</sup>

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Received November 21, 1995; Revised Manuscript Received February 5, 1996<sup>⊗</sup>

ABSTRACT: The backbone dynamics of the coiled-coil leucine zipper domain of c-Jun have been studied using proton-detected two-dimensional  ${}^{1}H^{-15}N$  NMR spectroscopy. Longitudinal  $(T_1)$  and transverse  $(T_2)^{15}$ N relaxation times, together with  $\{^{1}H\}^{15}$ N NOEs, were measured and analyzed by considering the protein to approximate a prolate ellipsoid. An analysis of the  $T_1/T_2$  ratios for residues in the well-structured section of the protein showed that a model for the spectral density function in which the protein is considered to reorient anisotropically fitted the data significantly better than an isotropic model. Order parameters  $(S^2)$  in the range 0.7–0.9 were observed for most residues, with lower values near the C-terminus, consistent with fraying of the two helices comprising the coiled-coil. Because nearly all of the N-H vectors have small angles to the long axis of the molecule, there was some uncertainty in the value of the rotational diffusion coefficient  $D_{par}$ , which describes rotation about the long axis. Thus, an alternative method was examined for its ability to provide independent estimates of  $D_{par}$  and  $D_{perp}$  (the diffusion coefficient describing rotation about axes perpendicular to the long axis); the translational diffusion coefficient  $(D_1)$ of the protein was measured, and hydrodynamic calculations were used to predict  $D_{par}$  and  $D_{perp}$ . However, the derived rotational diffusion coefficients proved to be very dependent on the hydrodynamic model used to relate  $D_t$  to  $D_{par}$  and  $D_{perp}$ , and consequently the values obtained from the  $T_1/T_2$  analysis were used in the order-parameter analysis. Although it has previously been reported that the side chain of a polar residue at the dimer interface, Asn22, undergoes a conformational exchange process and destabilizes the dimer, no evidence of increased backbone mobility in this region was detected, suggesting that this process is confined to the Asn side chain.

It has become clear in recent years that the highly specific molecular recognition processes which occur in biological systems are intimately dependent on the dynamic properties of the species concerned [see, for example, Bennett and Huber (1983), Karplus and McCammon (1983), Ringe and Petsko (1985), and Williams (1989)]. Such processes all comprise a delicate balance of enthalpic and entropic contributions (Page & Jencks, 1971; Jencks, 1981; Fersht, 1987; Williams *et al.*, 1991), and an understanding of the nature of these motions will undoubtedly assist in, for example, the design of specific inhibitors of protein function.

The protein c-Jun is a eukaryotic transcriptional activator, deregulated expression of which has been implicated in the neoplastic transformation of cells (Angel & Herrlich, 1994). c-Jun is a member of the basic domain leucine zipper (bZIP) class of DNA-binding proteins; these proteins consist of two distinct domains, a highly basic DNA-binding domain and a leucine zipper domain (Landschulz *et al.*, 1988). This leucine zipper domain mediates protein dimerization (both homodimerization and heterodimerization with other bZIP proteins), which juxtaposes the two DNA-binding domains so that they are able to bind their cognate enhancer sequence. These sequences all have dyad symmetry; each half of the dimer thus occupies one half-site on the DNA (Hurst, 1994). Protein dimerization is therefore a prerequisite for DNA

binding, so the activity of these bZIP proteins is regulated not only by the interactions between the protein and DNA but equally by the protein—protein interactions between the leucine zipper domains (Alber, 1992).

Dimerization of leucine zipper proteins occurs via the formation of a parallel coiled-coil of  $\alpha$ -helices. The leucine zipper is characterized by a heptad repeat of leucine residues (Landschulz et al., 1988), and, following conventional nomenclature for such repeats  $[(abcdefg)_n]$ , the leucine residues are found at position d (Figure 1). Another heptad repeat of hydrophobic residues is found at position a, and together these a- and d-position residues form a hydrophobic dimer interface. It has been suggested that the coiled-coil is further stabilized by polar groups in the positions adjacent to the hydrophobic interface (e and g) forming interhelical ion-pairs (McLachlan & Stewart, 1975; Zhou et al., 1994), although the relative importance of electrostatic interactions in these dimers is presently unclear (Junius et al., 1996; Lumb & Kim, 1995). Note, however, that these polar residues contribute to the stability of the hydrophobic interface via the packing of their methylene groups against the residues in the **a** and **d** positions (O'Shea et al., 1991).

A notable feature of most bZIP proteins is a conserved a-position polar residue (usually Asn) at the hydrophobic interface (Hurst, 1994). X-ray crystallographic studies of the GCN4 leucine zipper (O'Shea *et al.*, 1991) showed that this Asn residue adopts an asymmetric conformation in the otherwise generally symmetrical structure and that its side chain packs more loosely against adjacent residues than do other a-position side chains. Replacement of this Asn residue with a Val dramatically stabilizes the coiled-coil (Harbury

<sup>&</sup>lt;sup>†</sup> This work was supported by a research grant to G.F.K. from the National Health and Medical Research Council of Australia. J.P.M. is supported by an Australian Research Council Postdoctoral Research Fellowship. G.L.S. thanks the Wellcome Trust for financial support.

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<sup>&</sup>lt;sup>®</sup> Abstract published in Advance ACS Abstracts, March 15, 1996.

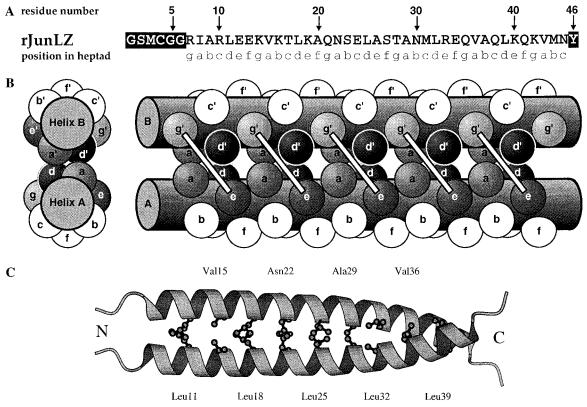


FIGURE 1: (A) Amino acid sequence of the rJunLZ monomer (Riley *et al.*, 1994). The numbering for rJunLZ is shown, as well as the position of each residue in the heptad repeat. Non-native residues are indicated by reverse type. (B) Schematic representation of a parallel, two-stranded coiled-coil, with each residue denoted by a sphere. For simplicity, the supercoiling of the two helices is not shown. (C) Molscript (Kraulis, 1991) diagram of the sJunLZ homodimer (*i.e.*, rJunLZ without the residues Gly1, Ser2, and Met3), showing the **a**- and **d**-position residues at the dimer interface (Junius *et al.*, 1996).

et al., 1993). We have recently shown that a similar situation exists for the homodimeric Jun leucine zipper (Junius et al., 1995), in which the homologous Asn (Asn22 in the recombinant peptide used in this study; Asn291 in native c-Jun) is involved in a conformational exchange process, thereby destabilizing the dimer in comparision to an Asn → Leu mutant. It has been suggested that the destabilization caused by this Asn residue may help to make dimerization reversible (O'Shea et al., 1991), thus facilitating the homo-/heterodimer exchange reactions crucial to the biological function of these transcription factors (Alber, 1992; Мс-Knight, 1991).

Nuclear magnetic resonance (NMR) measurements of <sup>15</sup>N (and to a lesser extent, <sup>13</sup>C) nuclear spin relaxation times have been used widely in recent years to investigate the motions of individual atoms and domains within proteins on a time scale faster that the overall tumbling time of the molecule (Nirmala & Wagner, 1988, 1989; Kay *et al.*, 1989; Palmer *et al.*, 1991b). For example, Cheng *et al.* (1994) characterized changes in the backbone flexibility of FK506-binding protein following the binding of FK506, and Barbato *et al.* (1992) showed that the central linker region of calmodulin is very flexible in solution, in contrast to the ordered helical structure observed in the solid state by X-ray crystallography.

In this study, we have used <sup>15</sup>N relaxation measurements to probe the backbone dynamics of the homodimeric Jun leucine zipper, the solution structure of which we have recently solved (Junius *et al.*, 1996). This work forms a part of our ongoing attempt to elucidate the balance of forces which determines specificity, affinity, and kinetics of leucine zipper formation. In particular we were interested in whether

or not the destabilization of the native zipper by the interfacial Asn residue was manifested as an increase in backbone flexibility in that region of the coiled-coil. A method for providing an independent experimental estimate of the overall molecular tumbling time(s) is also examined: the translational diffusion coefficient of the c-Jun leucine zipper was measured using pulsed field gradient (PFG) NMR (Stejskal & Tanner, 1965; Kuchel & Chapman, 1991; Dingley *et al.*, 1995) and used to derive estimates of the corresponding rotational correlation time(s).

## MATERIALS AND METHODS

*Materials*. Sodium 3-(trimethylsilyl)[2,2,3,3- $^2$ H]propionate ( $d_4$ -TSP) was obtained from Fluka AG (Buchs, Switzerland), while sodium azide and D<sub>2</sub>O (99.99% isotopic purity) were purchased from Sigma Chemical Co. (St. Louis, MO). Human [98% U- $^{15}$ N, $^{13}$ C]ubiquitin was purchased from VLI Research (Wayne, PA). All other chemicals used were of analytical grade.

*General*. Production of recombinant c-Jun leucine zipper (rJunLZ) has been described previously (Riley *et al.*, 1994). This peptide differs from a synthetic version used in our previous studies in that rJunLZ has three extra non-native residues at the N-terminus (46 residues in total, see Figure 1A). NMR experiments were performed on a sample containing 2.8 mg of uniformly  $^{15}$ N-labeled rJunLZ dissolved in a solution composed of 450 μL of H<sub>2</sub>O, 50 μL of D<sub>2</sub>O, 5 μL of 10 mM  $^{4}$ -TSP, and 5 μL of 100 mM NaN<sub>3</sub>, pH 3.6. [U- $^{13}$ C,  $^{15}$ N]Ubiquitin was prepared as a solution of 5 mg of protein in 450 μL of H<sub>2</sub>O, 50 μL of D<sub>2</sub>O, and 25 μM chloramphenicol, pH 4.0. All NMR measurements were carried out at 310 K on a Bruker AMX600 spectrometer,

sample did not exceed 18 mm.

except for the PFG diffusion measurements, which were performed at 298 K on a Bruker DRX500 equipped with an actively-shielded gradient probe. The magnitude of the pulsed field gradients has been shown to be linear over a length of 20 mm; the samples used for diffusion measurements were therefore prepared in 5-mm susceptibility-matched microcells (Shigemi, Japan), so the depth of the

<sup>15</sup>N Relaxation Theory. The relaxation of <sup>15</sup>N magnetization is dependent primarily on the dipolar interaction with its attached proton(s) and on its chemical shift anisotropy. Equations describing  $T_1$ ,  $T_2$ , and the { $^1$ H} $^{15}$ N NOE in terms of spectral density functions have been given previously (Abragam, 1961; Stone *et al.*, 1992). These equations require a value for the N−H bond length which was assumed to be 1.02 Å in this work. The magnitude of the  $^{15}$ N chemical shift anisotropy ( $\sigma_{par} - \sigma_{perp}$ ) has been shown to be dependent on the conformation of the polypeptide chain (Shoji *et al.*, 1989, 1990); since rJunLZ is helical, a value of −160 ppm was used in our calculations.

The spectral density,  $J(\omega_i)$ , depends on both the overall motion of the protein and the local motions occurring within the protein. The most common approach toward extracting motional parameters from <sup>15</sup>N relaxation measurements uses the model-free formalism of Lipari and Szabo (1982a,b). Lipari and Szabo showed that when the overall motion is isotropic and the internal motions are much faster than the rate of overall tumbling, a good model for the spectral density function is

$$J(\omega_i) = \frac{2}{5} \left[ \frac{S^2 \tau_{\rm M}}{1 + (\omega_i \tau_{\rm M})^2} + \frac{(1 - S^2)\tau}{1 + (\omega_i \tau)^2} \right]$$
(1)

where  $\tau_{\rm M}$  is the correlation time for overall tumbling of the protein. The order parameter,  $S^2$  ( $0 \le S^2 \le 1$ ), describes the extent of restriction of local motions at individual <sup>15</sup>N nuclei, and  $1/\tau = 1/\tau_{\rm M} + 1/\tau_{\rm e}$ , where  $\tau_{\rm e}$  is the (residue-specific) effective correlation time for the local motions.

This model only applies to proteins that tumble isotropically in solution. For a protein which tumbles anisotropically, it is not strictly valid to treat the overall motion and the internal motions separately. If, however, the internal motions occur on a time scale that is much faster than the rate of overall tumbling, then treating the two types of motions independently is a reasonable approximation (Lipari & Szabo, 1982b). In this case, for an axially symmetric molecule with different rotational diffusion coefficients parallel ( $D_{\rm par}$ ) and perpendicular ( $D_{\rm perp}$ ) to the unique axis of the molecule, the spectral density function may be written as (Woessner, 1962; Huntress, 1968; Zheng *et al.*, 1995)

$$J(\omega_i) = \frac{2}{5}S^2 \left[ \frac{A_1 \tau_1}{1 + (\omega_i \tau_1)^2} + \frac{A_2 \tau_2}{1 + (\omega_i \tau_2)^2} + \frac{A_3 \tau_3}{1 + (\omega_i \tau_3)^2} \right] + \frac{2}{5}(1 - S^2) \left[ \frac{A_1 \tau_1'}{1 + (\omega_i \tau_1')^2} + \frac{A_2 \tau_2'}{1 + (\omega_i \tau_2')^2} + \frac{A_3 \tau_3'}{1 + (\omega_i \tau_3')^2} \right] (2)$$

where

$$A_1 = 0.75 \sin^4 \alpha \tag{3}$$

$$A_2 = 3\sin^2\alpha\cos^2\alpha\tag{4}$$

$$A_3 = (1.5\cos^2\alpha - 0.5)^2 \tag{5}$$

and  $\alpha$  is the angle between the N–H vector and the unique axis of the molecule.  $\tau_i'$  is given by  $1/\tau_i' = 1/\tau_i + 1/\tau_e$ , where  $\tau_i$  (i = 1, 2, or 3) are overall correlation times for the protein, given as combinations of the two rotational diffusion coefficients:

$$\tau_1 = (2D_{\text{perp}} + 4D_{\text{par}})^{-1}$$
 (6)

$$\tau_2 = (5D_{\text{perp}} + D_{\text{par}})^{-1} \tag{7}$$

$$\tau_3 = (6D_{\text{perp}})^{-1} \tag{8}$$

The residue-specific parameters  $A_1$ ,  $A_2$ , and  $A_3$  may be determined from the coordinates of the three-dimensional structure of the protein (see below). Thus, there are four parameters remaining to be determined: the two global rotational diffusion coefficients ( $D_{\text{perp}}$  and  $D_{\text{par}}$ ), the order parameter  $S^2$ , and the effective correlation time for internal motions,  $\tau_e$ .

15N Relaxation Experiments. The pulse sequences used for the measurement of  $T_1$  and  $T_2$ , together with one of the experiments used to measure the NOE, are essentially those used by Kördel *et al.* (1992). These spectra were recorded using the sensitivity-enhancement procedure developed by Palmer *et al.* (1991a,b), which allows two orthogonal components of the magnetization to be recorded simultaneously, giving two independent pure-phase data sets after suitable deconvolution. Such data sets may be added together to yield a theoretical improvement in signal-to-noise of  $\sqrt{2}$  over a conventional spectrum recorded in the same total time; in this case, however, the two data sets were not co-added but instead used as independent duplicates. Thus, two estimates of  $T_1$ ,  $T_2$ , and the NOE may be obtained in the same time as a single conventional experiment.

Transverse relaxation times were measured by monitoring the peak height as a function of the length of an <sup>15</sup>N spinlocking pulse. Thus, in principle, the measured relaxation times,  $T_{1\rho}$ , differ from  $T_2$  since  $T_{1\rho}$  is dependent on the angle between the axis of the spin-locking pulse and the axis of the effective field. In this work the rf field strength of the spin-locking pulse was 2.9 kHz which locks the magnetization about an axis within  $\pm 9^{\circ}$  of the transverse plane. Under these circumstances, and in the absence of low-frequency perturbations,  $T_{1\rho}$  should be equivalent to  $T_2$ , allowing the distinction between the two to be dropped. During the variable delay of the  $T_1$  experiment,  $\tau$ , and the spin-locking pulse of the  $T_2$  experiment,  $\tau$ , synchronous proton decoupling was applied using the GARP-1 sequence (Shaka et al., 1985) to remove the effects of cross-correlation between dipolar and chemical shift anisotropy (CSA) relaxation mechanisms from the data (Boyd et al., 1990). The  $T_1$  spectra were recorded with  $\tau$  delays of 50, 150, 350, 600, 1000, 1500, 2000, 2500, and 3500 ms, while the  $T_2$  measurements used values of 10, 30, 60, 100, 150, 250, 500, 750, and 1000 ms. Measurement of the {1H}15N NOE requires the acquisition of two experiments, one with <sup>1</sup>H decoupling applied during the recycle delay and one without. The NOE was measured using two different pule sequences; the reason for this is discussed in the Results. In the first experiment (Kördel et al., 1992), water suppression was achieved using a purge pulse, while in the second experiment all proton pulses are

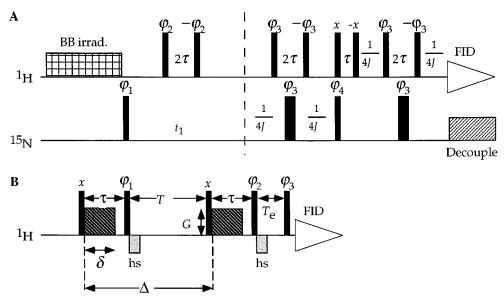


FIGURE 2: Pulse sequences for the measurement of (A) the  $\{^1H\}^{15}N$  NOE, using  $1-\bar{1}$  pulses for water suppression (Sørensen *et al.*, 1995) and (B) the translational diffusion coefficients of rJunLZ and ubiquitin (Gibbs & Johnson, 1991; Waldeck *et al.*, 1993). In A, the phase cycling was  $\varphi_1 = (x, -x)$ ;  $\varphi_2 = (x, -x, y, -y)$ ;  $\varphi_3 = 16(x, -x)$ ;  $\varphi_4 = 2(y, -y)$ ; acq = (x, -x, -x, x). The broadband  ${}^1H$  irradiation used to generate the NOE consisted of a WALTZ-16 broadband decoupling sequence. Quadrature detection was achieved using TPPI on  $\varphi_1$ . In B, the phase cycling was  $\varphi_1 = (x, -x)$ ;  $\varphi_2 = 2(x)$ , 2(-x);  $\varphi_3 = 4(x)$ , 4(y), 4(-x), 4(-y); acq = (x, -x, -x, x, y, -y, -y, y, -x, x, x, -x, -y, y, y, -y). Negative homospoil gradient pulses (hs) were used to eliminate any transverse magnetization remaining at the beginning of the longitudinal storage periods. The magnetic field gradients used for diffusion labeling were applied for time  $\delta$  with an amplitude of G cm $^{-1}$ . The time period  $\tau$  was kept constant to eliminate any contribution to signal decay from  $T_2$  relaxation and  $T_2$  modulation (Dingley *et al.*, 1995).  $\Delta$  is the total time allowed for molecular diffusion, and  $T_2$  is a delay to allow for the dissipation of eddy-current effects arising from the field gradients prior to acquisition.

replaced with 1-1 (jump-return, JR) pulses (Figure 2A; Sørensen *et al.*, 1995).

All spectra were recorded with spectral widths of 802 and 5747 Hz in  $F_1$  and  $F_2$ , respectively, using acquisition times of 79 and 356 ms in  $t_1$  and  $t_2$ , respectively. The carrier frequency was set to the frequency of the water resonance in  $F_2$  and to the center of the <sup>15</sup>N spectrum in  $F_1$ . The amide proton resonances of Gly5 and Gly6 were folded in the <sup>15</sup>N dimension in order to increase spectral resolution in  $F_1$  (see Figure 3). INEPT delays were set to 2.8 ms. Water suppression was achieved using a pair of orthogonal purge pulses (Messerle et al., 1989) in the  $T_1$  and  $T_2$  experiments, together with very weak selective irradiation of the water resonance during part of the recycle delay. For the sensitivity-enhanced NOE experiment, a single purge pulse was applied immediately prior to the first <sup>15</sup>N pulse. In all cases, a post-acquisition filter was applied to reduce further the intensity of the water resonance (Marion et al., 1989). Quadrature detection was achieved in  $t_1$  using timeproportional phase incrementation (TPPI; Marion & Wüthrich, 1983). The total recycle delay between transients was set to 4.2 s for the  $T_1$  and  $T_2$  experiments and to 12 s for the NOE experiments, although experiments were recorded with shorter recycle delays for comparison. The number of scans per  $t_1$  increment was 32 for the  $T_1$  and  $T_2$  experiments and 32-64 for the NOE experiment. The JR NOE experiment was carried out twice with the JR delay tuned to give different intensity maxima (130 and 103 µs gave maxima at 7.9 and 8.7 ppm, respectively), as the bandwidth over which reasonable sensitivity is obtained in this experiment is rather narrow (Sørensen et al., 1995). These two experiments were both duplicated to provide an error estimate for data recorded at each offset; weighted means were calculated subsequently from each pair of measurements. This procedure takes into account the offset dependence of the signal intensities in the JR NOE experiment.

PFG Diffusion Experiments. Translational diffusion coefficients for both rJunLZ and ubiquitin were determined using the PFG longitudinal eddy-current delay (LED) pulse sequence (Figure 2B; Gibbs & Johnson, 1991; Waldeck *et al.*, 1993). Each diffusion measurement was obtained from a series of twelve PFGLED spectra in which the delay periods  $\tau$  (20 ms),  $\Delta$  (50 ms), and  $T_e$  (4 ms) and the magnitude of the gradients (G, 11.0 G cm<sup>-1</sup>) were held constant, and the length of the field gradient pulses was incremented in 1.75-ms steps (from 0 to 19.25 ms in the final spectrum). A "dummy" experiment (G = 0 G cm<sup>-1</sup>) was acquired at the beginning of each series to ensure the sample had reached thermal equilibrium.

Data Processing. Data were processed on a Silicon Graphics Indigo R4000 computer, using a combination of commercial software (UXNMR) and programs written inhouse. The <sup>1</sup>H-frequency scale of all spectra was directly referenced to TSP at 0.00 ppm, while the <sup>15</sup>N-frequency scale was indirectly referenced to liquid NH<sub>3</sub> via the <sup>1</sup>H frequency of the TSP resonance (Live et al., 1984). Cross-peaks in the <sup>1</sup>H-<sup>15</sup>N correlation spectra were well-resolved, except for a small amount of overlap observed between the signals from residues Ala9, Leu11, Gln35, and Met44 (see Figure 3). Linear prediction was used in  $t_1$  to extend the data from 128 real points to 192 real points. The data were zero-filled once in each dimension, multiplied by weighting functions (Lorentz-Gauss function in t2 and a squared shifted-sinebell in  $t_1$ ), and then transformed to give final data matrices of 2048  $(F_2) \times 128 (F_1)$  real points. Polynomial base line corrections were applied to the processed spectra in  $F_2$ .

All diffusion experiments were recorded using 8192 complex data points and a spectral width of 6000 Hz. Free induction decays were multiplied by a decaying exponential function with a decay constant of 2 Hz before Fourier transformation.

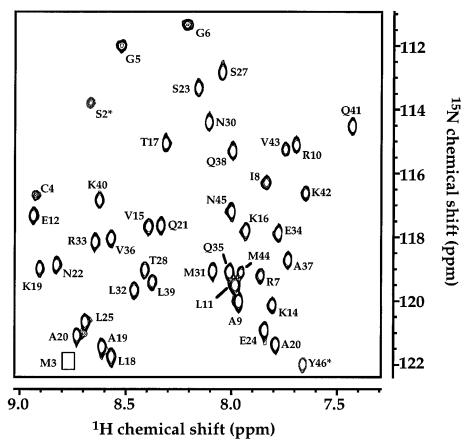


FIGURE 3: Example of a sensitivity-enhanced  $\{^1H\}^{15}N$  NOE spectrum of rJunLZ. The signals from Gly5 and Gly6 are aliased in the  $F_1$  dimension. Ser2 and Tyr46 have negative cross-peak intensities (marked with an asterisk) due to their large, negative NOEs, and Met3 shows zero intensity due to its NOE of -1. It can be seen that there is very little overlap which could adversely affect measured peak intensities in the relaxation experiments. The resonance of Gly1 cannot be detected under the experimental conditions.

Calculation of Relaxation Rates and NOEs. Cross-peak heights were measured using the program XEASY (Bartels et al., 1995), which was kindly provided by Professor K. Wüthrich.  $T_1$  values were calculated for each residue from three-parameter nonlinear fits of the experimental data to eq 9:

$$I(\tau) = I_{\infty} - [I_{\infty} - I_0] \exp(-\tau/T_1)$$
(9)

 $T_2$  values were likewise obtained from three-parameter fits to the equation

$$I(\tau) = I_{\infty} + I_0 \exp(-\tau/T_2)$$
 (10)

In these equations  $I_0$  and  $I_\infty$  are the cross-peak intensities at zero- and infinite-time, respectively. Nonlinear least-squares curve-fitting was carried out using the program KaleidaGraph 3.0 (Synergy Software, Reading, PA). Uncertainties in the fitted relaxation times were taken to be the standard errors given by the program.  $T_1$  and  $T_2$  values were calculated for each duplicate dataset separately, and from these, weighted average means/grouped SDs were then derived. Note that rms base line noise levels were not used to estimate the error in peak heights, as we found that this would have led to significantly underestimated errors. A similar observation was made recently by Skelton *et al.* (1993). The  $\{^1H\}^{15}N$  NOEs were calculated as fractional enhancements according to eq 11

$$f_1\{S\} = (I_{\text{sat}} - I_{\text{ref}})/I_{\text{ref}}$$
 (11)

where  $I_{\text{sat}}$  and  $I_{\text{ref}}$  are the cross-peak intensities in the presence

and absence of <sup>1</sup>H saturation, respectively. The sensitivity-enhanced NOE experiment was repeated four times (see Results), and the peak heights from the resulting eight datasets were averaged to yield error estimates of the peak heights. For the JR NOE experiment, a similar method was used to calculate the NOEs.

Analysis of <sup>15</sup>N Relaxation Data. The  $T_1/T_2$  ratios were fitted to different models describing the tumbling of rJunLZ, in order to determine which model best describes the molecule. The models for overall motion were fitted to the  $T_1/T_2$  data by minimizing the error function

$$\chi^{2} = \sum_{i} \left[ \frac{(T_{1}/T_{2})_{\text{calc},i} - (T_{1}/T_{2})_{\text{obs},i}}{\sigma_{\text{obs},i}} \right]^{2}$$
 (12)

where  $(T_1/T_2)_{\text{obs},i}$  and  $(T_1/T_2)_{\text{calc},i}$  are the observed and calculated values of the  $T_1/T_2$  ratio, respectively, and  $\sigma_{\text{obs},i}$  is the error in  $(T_1/T_2)_{\text{obs},i}$ . The sum is carried out over the residues that are found in "well-structured" regions of the protein (see below). To calculate  $\chi^2$  using an anisotropic tumbling model, the angle between each N-H vector and the unique axis of the ellipsoid,  $\alpha_i$ , must be known. These angles were calculated from the atomic coordinates of the seven best solution structures of rJunLZ (Brookhaven Protein Data Bank, 1jun; Junius *et al.*, 1996) using the following procedure. The coordinates were first used to calculate the inertial tensor for the molecule; this tensor was subsequently diagonalized. Since the eigenvector of the smallest eigenvalue of inertial tensor corresponds to the long axis of the molecule, the angle between each N-H vector and this axis

can be calculated from the dot product of the two vectors. This procedure was repeated for each solution structure, giving a number of estimates for  $\alpha_i$ . These estimates were then averaged, and the uncertainty in  $\alpha_i$  was taken from the standard deviation. Each estimate of  $\alpha_i$  actually comprised an average of two symmetrically related residues since rJunLZ is a symmetric dimer.

Residues i were excluded from the  $T_1/T_2$  fit (Barbato et al., 1992) when both

(a) 
$$NOE_i < -0.35$$
 (13a)

and

(b) 
$$T_{2,i} < \langle T_2 \rangle - \sigma_{T_2}$$
 and  $\frac{(T_{2,i} - \langle T_2 \rangle)}{T_{2,i}} > \frac{3(\langle T_1 \rangle - T_{1,i})}{T_{1,i}}$  (13b)

where  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  are the mean  $T_1$  and  $T_2$  values taken over all residues and  $\sigma_{T_2}$  is the standard deviation of the  $T_2$  data.

The goodness of fit of the various models for rJunLZ tumbling was assessed using an F statistic. To compare  $\chi^2$  from two models with  $\nu_1$  and  $\nu_2$  degrees of freedom ( $\nu_1 > \nu_2$ ), the F-test statistic is

$$F(\nu_1, \nu_2) = \nu_2 \left( \frac{\chi^2(\nu_1) - \chi^2(\nu_2)}{\chi^2(\nu_2)} \right)$$
 (14)

where  $\chi^2(\nu_i)$  is the value of  $\chi^2$  for the model with  $\nu_i$  degrees of freedom. A small F statistic indicates that there is no difference between the ability of the two models to explain the data, and a large F statistic indicates that the more complex model is justified.

Calculation of Translational Diffusion Coefficients. The signal intensity  $(R_t)$  recorded in a PFG diffusion experiment is given by

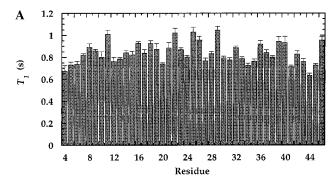
$$R_{\rm t} = R_{\infty} + R_0 \exp\{-\gamma^2 G^2 D \delta^2 (\Delta - \delta/3)\} \qquad (15)$$

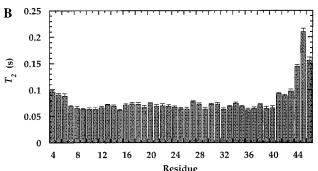
where G and  $\delta$  are the strength and duration of the gradient pulses, respectively,  $\Delta$  is the time between gradient pulses,  $\gamma$  is the magnetogyric ratio of the observed nucleus, and  $R_{\infty}$  and  $R_0$  are the normalized resonance intensities at infinite-and zero-time, respectively. A nonlinear least-squares fit of the PFG data yields the translational diffusion coefficient and an estimate of its error. For both rJunLZ and ubiquitin, several resonances were used to determine diffusion coefficients and weighted means were calculated.

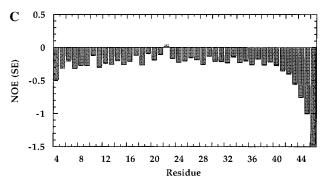
The molecular masses (M) of both ubiquitin and rJunLZ were estimated from their measured diffusion coefficients  $(D_t)$ , using the equation (Cantor & Schimmel, 1980; Dingley *et al.*, 1995)

$$M = \left(\frac{kT}{6\pi\eta F D_{\rm t}}\right)^3 \left(\frac{4\pi N_{\rm a}}{3[\bar{\nu}_2 + \delta\bar{\nu}_1]}\right) \tag{16}$$

where  $\eta$  is the viscosity of the solvent, F is the Perrin factor which relates to molecular shape [see Cantor and Schimmel (1980) and Dingley *et al.* (1995)],  $N_a$  is Avogadro's number,  $\bar{\nu}_2$  is the partial specific volume of the protein,  $\delta_1$  is the fractional amount of water bound to the protein (typically,







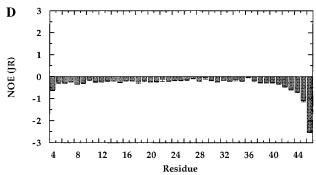


FIGURE 4: Derived values of (A)  $T_1$ , (B)  $T_2$ , and (C, D)  ${}^{1}H{}^{15}N$  NOE for the rJunLZ dimer. The uncertainties are plotted as standard errors. C shows the NOEs derived from the sensitivity-enhanced NOE experiment, while D shows the NOEs derived from the JR NOE experiment. Note that values for residues Ser2 and Met3 are not given (see text).

0.3–0.4 g of H<sub>2</sub>O per g of protein), and  $\bar{\nu}_1$  is the partial specific volume of the solvent.

#### RESULTS AND RELAXATION ANALYSIS

Determination of the Model for Overall Motion. Figure 4 shows the derived  $T_1$ ,  $T_2$ , and NOE values; NOE data determined from both the sensitivity-enhanced and JR NOE experiments are shown for comparison. The average standard errors were 3.3% ( $T_1$ ), 4.0% ( $T_2$ ), 5.6% (sensitivity-enhanced NOE), and 16% (JR NOE). Although the errors were significantly larger for the JR NOE experiment

compared with the sensitivity-enhanced NOE experiment, we chose to combine the data from both experiments for the model-free analysis. For two residues, the {1H}15N NOE is more positive than the maximum value predicted from theory; this has been observed in other studies [e.g., Rischel et al. (1994)]. In particular, this was noted for Asn22 when the NOE was measured using the sensitivity-enhanced pulse sequence. It is possible for the combination of chemical exchange between the amide proton and solvent water, and the slow longitudinal relaxation of the water magnetization, to lead to erroneously high NOE measurements (Grzesiek & Bax, 1993). If saturation of the water magnetization is minimized, then this problem can be reduced; one way of achieving this aim is to use the JR NOE sequence (Figure 2A). The use of this sequence reduced the size of the positive NOE measured for Asn22; however, it still remained larger than expected from theory.

The first step in the analysis of the relaxation data is to determine whether the shape of the protein may be best approximated by a sphere or by a symmetric ellipsoid so that either eq 1 or eq 2 may be chosen to analyze the data. In the case of rJunLZ, visual inspection of the threedimensional structure suggests that the overall motion of the protein should be modeled using a prolate ellipsoid. This can be confirmed by calculating the axial ratio of the inertial tensor; in the case of rJunLZ the axial ratio of the inertial tensor is 2.78:2.75:1 (see below). Although both visual inspection and the use of the inertial tensor suggest that an ellipsoidal model for overall motion should be used, a more quantitative approach to choosing the model is preferable. This can be achieved by fitting the  $T_1/T_2$  ratio using the different models; the model which gives the best fit to the data is deemed the most suitable (Zheng et al., 1995). The  $T_1/T_2$  ratio is used in this procedure since, in the absence of slow internal motions ( $\tau_e \le 100$  ps,  $S^2 > 0.7$ ), the  $T_1/T_2$  ratio is independent of both  $S^2$  and  $\tau_e$  (Kay et al., 1989; Clore et al., 1990) and depends only on the parameters describing overall motion. The error function described in Materials and Methods (eq 12) was minimized, with the summation including only the residues which are found in well-structured regions of the protein (see below). Since the solution structure was calculated using constraints derived largely from a synthetic peptide, which lacked residues Gly1, Ser2, and Met3 of rJunLZ, angles could not be derived for these residues, and they were excluded from these, and all further, calculations. 3D NOESY-HMQC data (Junius et al., 1995), together with the raw 15N relaxation data, suggest that these residues are highly mobile and probably completely unstructured. In addition, other residues were excluded using the criteria described in Materials and Methods (eqs 13a and 13b). On this basis, Cys4 and the C-terminal residues Lys42-Tyr46 were excluded from the  $T_1/T_2$  calculations.

The models for the overall motion tested in this way included (i) an isotropic overall tumbling model; (ii) an anisotropic ellipsoidal tumbling model with the ratio of  $D_{\rm par}$  to  $D_{\rm perp}$  fixed to 2.77:1 (from the inertial tensor calculation); (iii) an anisotropic ellipsoidal tumbling model with both  $D_{\rm par}$  and  $D_{\rm perp}$  varied freely. Table 1 shows  $\chi^2$ , the fitted parameters, and the degrees of freedom for each model. This analysis indicates that model iii achieves the best fit to the  $T_1/T_2$  data, but it does not indicate whether the improvement in the fit justifies the increased complexity of model iii. One criterion which can be used to answer this question is the statistical F test (eq 14). Comparing model iii with models

Table 1: Determination of the Most Appropriate Model for Overall Motion of the rJunLZ  $Dimer^a$ 

model	parameters	degrees of freedom	$\chi^2$	fitted parameters $(\times 10^{-7} \text{ s}^{-1})$
i	$D_{ m iso}$	36	577.2	$D_{\rm iso} = 1.69$
ii	$D_{\text{perp}}, D_{\text{par}}$ (fixed ratio)	36	476.7	$D_{\rm par} = 2.77 \times D_{\rm perp} = 4.04$
iii	$D_{ m perp}$ , $D_{ m par}$	35	405.1	$D_{\text{par}} = 2.80; D_{\text{perp}} = 1.56$

<sup>a</sup> As outlined in the text,  $\chi^2$  in eq 12 was minimized over all residues for different models of overall tumbling. Model i assumes isotropic reorientation in solution. Model ii allows for anisotropic tumbling (with axial symmetry) but fixes the ratio of  $D_{par}/D_{perp}$  from the inertial tensor calculation. Model iii allows both  $D_{par}$  and  $D_{perp}$  to vary freely in the minimization.

i and ii gives relatively large F statistics of 14.9 and 6.2, respectively. The probabilities that these statistics could have arisen simply by chance are  $7 \times 10^{-13}$  and  $2 \times 10^{-7}$ , respectively, indicating that model iii explains the data better than either model i or ii.

However, if model iii is to be used to analyze the relaxation data, then it is important to assess the precision of the rotational diffusion coefficients, in particular  $D_{par}$ , since the majority of the residues used in the calculation have N-H angles of less than ca.  $30^{\circ}$  to the long axis of the molecule. As a consequence, rotational diffusion about the long axis has less effect on the <sup>15</sup>N relaxation parameters than rotation about the two short axes. In addition, there is some uncertainty in the angle between each N-H vector and the principal axis of the protein; this uncertainty may be carried through to the estimates for the rotational diffusion coefficients. To determine the uncertainty in the rotational diffusion coefficients, 500 Monte Carlo simulations were performed which took into account both the uncertainty in the  $T_1/T_2$  ratio and the uncertainty in  $\alpha_1$ . The diffusion coefficients were determined as  $D_{\rm par} = (2.8 \pm 0.5) \times 10^7$  ${\rm m}^2~{\rm s}^{-1}$  and  $D_{\rm perp} = (1.56 \pm 0.05) \times 10^7~{\rm m}^2~{\rm s}^{-1}$  (using model iii above), where the uncertainties are the standard deviations from the Monte Carlo simulations. These results indicate that the estimates of the rotational diffusion coefficients are precise enough to use as initial estimates but that further refinement would be desirable.

Because of the uncertainty in the estimate for  $D_{par}$  we decided to try to obtain independent estimates of the magnitudes of  $D_{par}$  and  $D_{perp}$ . The simplest approach would be to calculate the rotational diffusion coefficients directly using standard hydrodynamic equations (Cantor & Schimmel, 1980). However, the reliability of this approach can suffer as a result of the approximations on which it is based; most notably, that the protein can be adequately modeled as a sphere or axially symmetric ellipsoid with a smooth surface. A more accurate approximation involves modeling the protein as a collection of spheres (point sources of friction) in a solvent continuum and calculating directly the elements of the rotational (and translational) diffusion tensor for that model (Torre & Bloomfield, 1981, 1989). The atomic coordinates of the protein (taken from either an NMR- or X-ray-derived structure) can be used to define the positions of the spheres—a useful approach is to use only  $C^{\alpha}$  atoms and to represent them as spheres with radius 3.5 Å. However, such models generally predict translational diffusion coefficients that are larger than experimentally observed values. The explicit inclusion of an partial layer of water can be used to correct for this difference, although it is

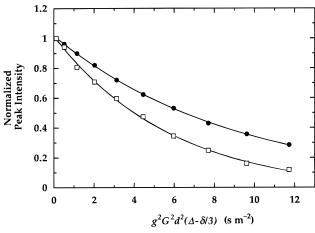


FIGURE 5: Peak intensities, from  $^1H$  PFGLED NMR experiments, for representative signals from rJunLZ (  $\bullet$  ) and ubiquitin (O), plotted as a function of  $\gamma^2 G^2 \delta^2 (\Delta - {}^{\delta}/_3)$ . Nonlinear regression of eq 15 onto the data (solid line) yielded the translational diffusion coefficients.

Table 2: Predicted Translational and Rotational Diffusion Coefficients for Ubiquitin from the Hydrodynamics Programs HYDRO and HI4 Together with the Experimentally Determined Translational Diffusion Coefficient<sup>a</sup>

	$\begin{array}{c} D_t \\ (\times 10^{10} \ m^2  s^{-1}) \end{array}$	$\begin{array}{c} D_{xx} \\ (\times 10^{-7}  \mathrm{s}^{-1}) \end{array}$	$\begin{array}{c} D_{yy} \\ (\times 10^{-7}{\rm s}^{-1}) \end{array}$	$D_{zz} \times 10^{-7}  \mathrm{s}^{-1})$
$HYDRO^b$	1.69	2.57	2.63	3.18
$HI_4{}^c$	1.77	5.35	6.07	9.47
$HYDRO + H_2O^{b,d}$	1.47	1.98	2.01	2.40
$D_{t}(obs)^d$	1.52			

<sup>a</sup> All calculations were carried out using the C<sup>α</sup> atom coordinates from the Brookhaven Protein Data Bank file 1ubq, so that the protein is represented as 76 spheres with 3.5 Å radii (T = 298 K,  $\eta = 8.904 \times 10^{-4}$  kg m<sup>-1</sup> s<sup>-1</sup>). Note that  $D_{zz}$  corresponds to  $D_{par}$  and that  $D_{xx} \approx D_{yy}$  corresponds to  $D_{perp}$  in models ii and iii. <sup>b</sup> Calculated using the modified Oseen tensor. <sup>c</sup> Calculated using the Oseen tensor. <sup>c</sup> Calculated for C<sup>α</sup> model with the addition of a 2 Å layer of water (88 molecules), added using InsightII (Biosym Inc., San Diego, CA). Each water molecule was represented as a sphere with a 1.6 Å radius. <sup>e</sup> From <sup>1</sup>H PFG NMR data.

difficult to predict *a priori* the amount of water required, as this can vary substantially from one protein to another (Venable & Pastor, 1988). An experimental measurement of the translational diffusion coefficient could potentially provide the information needed to calibrate the hydrodynamic calculation.

We have tested this approach using the small, approximately spherical protein ubiquitin (the ratio of the principal moments of the inertial tensor are 1.50:1.11:1). Figure 5 illustrates the <sup>1</sup>H PFG NMR diffusion data used to measure the translational diffusion coefficient of ubiquitin [(1.52  $\pm$  0.05)  $\times$  10<sup>-10</sup> m<sup>2</sup> s<sup>-1</sup>], and Table 2 gives the values of D<sub>t</sub> and of the rotational diffusion coefficients about three orthogonal axes  $(D_{xx}, D_{yy}, \text{ and } D_{zz})$  calculated using the hydrodynamic programs HYDRO (Torre, 1994) and HI4 (FORTRAN source code obtained from R. M. Venable and R. W. Pastor). It can be seen that, while the calculated translational diffusion coefficients both agree reasonably well with the experimental value, the predicted rotational diffusion coefficients differ substantially from each other. Schneider et al. (1992) have reported <sup>15</sup>N relaxation measurements of human ubiquitin, in which they derive a rotational correlation time of 4.1 ns (at 303 K), assuming isotropic reorientation. This corresponds to an isotropic rotational diffusion coefficient of  $4.1 \times 10^7 \text{ s}^{-1}$  ( $\tau_c = 1/(6D_{\text{rot}})$ ). Repeating the

Table 3: Predicted Translational and Rotational Diffusion Coefficients for rJunLZ from the Hydrodynamics Programs HYDRO and HI4 Together with Experimentally Determined Values<sup>a</sup>

	$D_{\rm t}$ (×10 <sup>10</sup> m <sup>2</sup> s <sup>-1</sup> )	$D_{xx} \times 10^{-7} \mathrm{s}^{-1})$	$\begin{array}{c} D_{yy} \\ (\times 10^{-7}  \mathrm{s}^{-1}) \end{array}$	$D_{zz} \times 10^{-7} \mathrm{s}^{-1}$
$HYDRO^b$	1.35	1.06	1.08	2.85
$HI4^c$	1.62	1.46	2.00	8.73
$HI4^b$	1.54	1.67	1.71	13.6
$HYDRO + H_2O^{b,d}$	1.26	0.97	1.00	2.43
$HI4 + H_2O^{b,e}$	1.37	1.25	1.33	4.95
$D_{\rm t}$ (obs)	1.36			

<sup>a</sup> All calculations were carried out using the  $C^{\alpha}$  atom coordinates from the NMR solution structure of sJunLZ, so that the protein is represented as 86 spheres with 3.5 Å radii. Note that  $D_{zz}$  corresponds to  $D_{par}$ , and  $D_{xx} \approx D_{yy}$  corresponds to  $D_{perp}$  in models ii and iii. <sup>b</sup> Calculated using the modified Oseen tensor. <sup>c</sup> Calculated using the Oseen tensor. <sup>d</sup> Calculated for  $C^{\alpha}$  model with the addition of a 1.5 Å layer of water (40 molecules), added using InsightII (Biosym Inc., San Diego, CA). Each water molecule was represented as a sphere with a 1.6 Å radius. <sup>e</sup> Calculated for  $C^{\alpha}$  model plus 40 molecules of water, as described above.

hydrodynamic calculations in Table 2 at 303 K gives values of  $7.9 \times 10^7$  and  $3.2 \times 10^7$  s<sup>-1</sup> using HI4 and HYDRO, respectively (again assuming isotropic tumbling). There are clearly significant differences in the way the two programs calculate rotational diffusion coefficients. Part of this difference lies in the use of the Oseen (HI4) versus modified Oseen (HYDRO) tensors for describing the nature of the hydrodynamic interaction between protein and solvent.

Note that in the case of ubiquitin, 88 explicitly included water molecules are necessary to reproduce the experimental translational diffusion coefficient. In comparison, previous work has shown that for the proteins hen egg white lysozyme and ribonuclease, 301 and 100 bound waters, respectively, were required in the hydrodynamic model to concur with experimental diffusion measurements (Venable & Pastor, 1988). The differences observed between proteins clearly show the potential danger in using hydrodynamic calculations to estimate rotational diffusion coefficients without having some independent data against which to calibrate the calculations. However, even with knowledge of the translational diffusion coefficient, there is clearly a dependence of the derived rotational diffusion coefficients on the mathematical model chosen to perform the calculations. In addition, while the measured and calculated values of  $D_t$  may be matched by the inclusion of bound water, the reliability of the rotational diffusion coefficients thus derived is probably dependent on the shape and rugosity of the proteinwater complex.

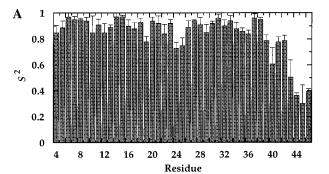
An attempt was made to apply this method to rJunLZ; Figure 5 shows the PFG diffusion measurements and Table 3 shows the calculated hydrodynamic parameters. Reasonable agreement with the measured  $D_{\rm t}$  [(1.36  $\pm$  0.01)  $\times$  10<sup>-10</sup> m<sup>2</sup> s<sup>-1</sup>] is obtained by HYDRO without the inclusion of any explicitly defined water molecules. However, the corresponding value of  $D_{\rm perp}$  (1.07  $\times$  10<sup>7</sup> m<sup>2</sup> s<sup>-1</sup>) is significantly different from that calculated using the  $T_1/T_2$  data above (1.56  $\times$  10<sup>7</sup> m<sup>2</sup> s<sup>-1</sup>). For HI4, good agreement of calculated  $D_{\rm t}$  with the measured value is obtained by adding 40 water molecules, but again the corresponding rotational diffusion coefficients are very different from the  $T_1/T_2$ -derived estimates. The observation that the rotational diffusion coefficients obtained by fitting the relaxation data do not agree with those obtained from translational diffusion measure-

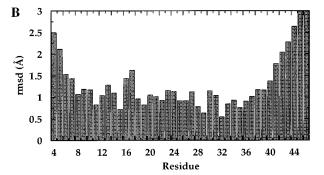
ments/hydrodynamic calculations is interesting. One possible cause for the discrepancy between these techniques is that protein aggregation is affecting the results. This explanation, however, is unlikely. The molecular mass estimated for rJunLZ obtained by substituting the measured value of  $D_t$ into eq 16 is  $11 \pm 2$  kDa, which is in good agreement with the actual molecular mass of 10.6 kDa. This result suggests that non-specific aggregation is probably not significant for the rJunLZ dimer under these conditions. In any case, it is important to realize that even if measurements of the rotational diffusion constants obtained from the <sup>15</sup>N relaxation data are biased in some sense by protein aggregation, these estimates are probably still the ones which will best enable information on internal motions to be extracted from the relaxation data (although if aggregation is significant, the interpretation of any extracted parameters will obviously be obscured). For this reason, and because of the variability of the hydrodynamic approach based on  $D_t$ , it was decided to use the estimates of  $D_{par}$  and  $D_{perp}$  derived from the  $T_1/T_2$ analysis for the subsequent fitting procedure.

*Model-Free Analysis.* Using the estimates of the rotational diffusion coefficients obtained in the preceding section, the model-free parameters  $S^2$  and  $\tau_e$  were calculated by minimization of the merit function (Stone *et al.*, 1992)

$$\chi_{i}^{2} = \left[ \frac{(T_{1,i}^{\text{obs}} - T_{1,i}^{\text{calc}})^{2}}{\sigma_{1,i}^{2}} + \frac{(T_{2,i}^{\text{obs}} - T_{2,i}^{\text{calc}})^{2}}{\sigma_{2,i}^{2}} + \frac{(\text{NOE}_{1,i}^{\text{obs}} - \text{NOE}_{1,i}^{\text{calc}})^{2}}{\sigma_{\text{NOE},i}^{2}} \right]$$
(17)

where  $P_i^{obs}$  is the observed value of a relaxation measurement for residue i,  $P_i^{\text{calc}}$  is the calculated value for the same parameter, and  $\sigma_i$  is the standard deviation in the measurement of  $P_i^{\text{obs}}$  ( $P_i = T_1$ ,  $T_2$ , NOE). The value of  $\chi_i^2$  was minimized for each residue, giving initial estimates for  $\tau_e$ and  $S^2$ . These estimates for the model-free parameters are dependent on the estimates for  $D_{par}$  and  $D_{perp}$ , which have been shown to contain a significant amount of uncertainty. Consequently the values for the diffusion constants were optimized in a grid search procedure. In this procedure an overall  $\chi^2$  value was calculated,  $\chi_t^2$ , by summation of  $\chi_i^2$ over all of the residues. The values of the diffusion constants were then varied systematically in a two-dimensional grid search until the minimum value for  $\chi_t^2$  was found. A 95% confidence interval for the resulting diffusion coefficients is  $D_{\rm par}=(2.6\pm0.3)\times10^7~{\rm s}^{-1}$  and  $D_{\rm perp}=(1.486\pm0.028)$  $\times 10^7$  s<sup>-1</sup>. Using these values for the diffusion coefficients, model-free parameters were extracted from the relaxation data and are displayed in Figure 6. Uncertainties in the calculated parameters were calculated by carrying out 500 Monte Carlo simulations. The Monte Carlo simulations were performed twice: the first simulation took into account only the errors in the relaxation data while the second simulation incorporated the uncertainties in both the relaxation data and the angles,  $\alpha_i$ . It was thought that since the value of  $\alpha_i$  has a large effect on the calculated values of  $T_1$  and  $T_2$ , large uncertainties in  $\alpha_i$  would lead to large uncertainties in  $S^2$ . Fortunately, in this case, the average standard deviation in S<sup>2</sup> increases only marginally from 0.04, when uncertainties in the angle are not accounted for, to 0.043 when the uncertainties in  $\alpha_i$  are included in the Monte Carlo simulations.





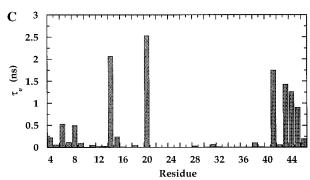


FIGURE 6: (A) Graph of the order parameter  $S^2$  against residue number for rJunLZ. The errors shown are standard deviations and are derived from 500 Monte Carlo simulations of the data. (B) Mean backbone rmsds for individual residues for the family of seven NMR-derived solution structures of rJunLZ (Junius *et al.*, 1996). Rmsds were obtained by superimposing structures pairwise onto the lowest energy structure and then averaging over the six different pairs. (C) Graph showing the internal correlation time  $\tau_e$  for each residue. No quantitative conclusions may be drawn from these values; consequently, error bars are not shown.

The observation that uncertainties in  $\alpha_i$  do not affect significantly the uncertainty in  $S^2$  can be understood by considering what happens when  $\alpha_i$  is decreased from its "true" value. The calculated value of  $T_1$  will increase, and the calculated value of  $T_2$  will decrease. It is not possible to alter  $S^2$  in a way which will simultaneously account for both these changes since  $S^2$  affects  $T_1$  and  $T_2$  in the same way (van Mierlo et al., 1993), and so the fitted value of  $S^2$ will not change very much. The value of  $\tau_e$  was found to be more sensitive to the uncertainty in  $\alpha_i$ ; the uncertainty in  $\tau_{\rm e}$  increased by 43% on average when the uncertainties in  $\alpha_i$  were included in the Monte Carlo simulations. As observed elsewhere [see, for example, Stone et al. (1993)] the uncertainities in  $\tau_e$  are large. This is a result of the insensitivity of  $\chi_i^2$  to the value of  $\tau_e$  and makes interpretation of the  $\tau_e$  data less reliable than interpretation of the order parameters. Consequently only the uncertainities in the order parameters are displayed and only these model-free parameters are interreted in terms of internal molecular motion.

#### DISCUSSION

Relatively few <sup>15</sup>N relaxation studies have been reported to date on proteins which are highly asymmetric. Barbato *et al.* (1992) studied calmodulin, which appears from the crystal structure to be a rigid dumbbell shape (Babu *et al.*, 1988). However, it was shown that, in solution, the protein could be adequately represented by two isotropically tumbling domains, implying that the linker region connecting the two domains is flexible; this allowed the simpler isotropic model (eq 1) to be used in the analysis of the relaxation data. Zink *et al.* (1994) and Zheng *et al.* (1995) used anisotropic models to analyze <sup>15</sup>N relaxation data recorded on human granulocyte colony-stimulating factor (rh-met-GCSF) and *trp* repressor, respectively.

The rJunLZ dimer is highly asymmetric (Junius et al., 1996), so a modified expression for the spectral density function (eq 2) was required to adequately interpret the <sup>15</sup>N NMR relaxation data. In this model, the value of the spectral density functions for a particular N-H unit are dependent on the angle made between the N-H vector and the principal axis of the protein, so that errors in the angles will be manifested in the final fitted parameters. Note that, although the use of a single angle for mobile residues may appear to be a contradiction, this condition is implicit in the assumption that the internal motions are much faster than the overall molecular tumbling (the angle  $\alpha$  is by definition an angle averaged by the fast internal motions). This decoupling of overall motion from internal motion appears to constitute a reasonable approximation for isotropically tumbling proteins (Lipari & Szabo, 1982a,b) and should hold for anisotropic proteins as well.

Because nearly all of the N-H vectors in the rJunLZ dimer point in a similar direction, at a small angle to the long axis of the molecule, the rotational diffusion coefficient  $D_{\rm par}$  may be poorly defined. Indeed, the ratio of  $D_{\rm par}/D_{\rm perp}$  is somewhat smaller than that predicted either from hydrodynamic calculations or from a simpler model where the protein is approximated by a prolate ellipsoid. An attempt was made to use the translational diffusion coefficient, measured using a PFG NMR experiment, to provide an independent estimate of  $D_{\rm par}$  and  $D_{\rm perp}$ , but it appears that the derived rotational diffusion coefficients are rather dependent on the model chosen to carry out the hydrodynamic calculations.

The calculated order parameters were consistently in the range 0.7-0.9 for all residues in the rJunLZ dimer, except for several residues at the C-terminus (Figure 6A), which shows substantially lower order parameters, as expected if the two helices constituting the coiled-coil fray at this end. This is consistent with the NMR data for rJunLZ (Junius et al., 1996), which reveals fewer NOEs in this region. The N-terminus is somewhat more ordered due to the disulfide bond at Cys 4. Figure 6B shows a plot of the backbone rmsds on a residue-by-residue basis for the calculated family of seven rJunLZ solution structures (Junius et al., 1996). This plot exhibits similar trends to the <sup>15</sup>N relaxation data. Taken together, these data are consistent with a model in which the conformational exchange process previously reported for rJunLZ is confined to the side chain of Asn22 and does not substantially affect the mobility of the peptide backbone. Figure 6C shows the derived values of the internal correlation time,  $\tau_e$ , for each residue, and there appears to be a substantial variation in this parameter without a discernable trend (other than that at the C-terminus).

Similar observations have been made in most studies of this type, and, typically, little significance has been placed on the values of this parameter.

It is interesting that the order-parameter profile (Figure 6A) shows no significant increase in backbone mobility in the region of the polar interfacial Asn22 residue, despite its demonstrated participation in a conformational exchange process (Junius et al., 1995) and its substantial destabilization of the coiled-coil dimer (Alber, 1992; Junius et al., 1995). Note however, that although there is no evidence for increased mobility of Asn22 on the nano- to picosecond time scale, this does not necessarily mean that this residue is not more mobile on a slower time scale. One might expect to see evidence for such slow motions as exchange contributions to  $T_2$ , although the size of a potential exchange contribution is dependent on the <sup>15</sup>N chemical shift difference between the exchanging sites, the exchange rate, and the field strength of the spin-locking field in the  $T_{1\rho}$  experiment (it is worth noting that the line width of the Asn22 cross-peak in the <sup>15</sup>N dimension of HSQC spectra recorded between 273 K and 310 K was indistinguishable from those of other residues in the structured region of the protein). Thus the failure to observe an exchange contribution does not necessarily imply that slow motions do not occur. Despite this caveat, the lack of additional mobility observed for Asn22 suggests that the instability conferred by this residue may result largely from its unfavorable location at the hydrophobic dimer interface rather than being a consequence of motional disorder introduced into the helical backbone of the zipper. Thus, the conformational exchange process previously observed for this residue (Junius et al., 1995) is probably confined to the Asn side chains. In fact, this motional disorder might provide some entropic compensation for its enthalpically unfavorable desolvation; this information will clearly be helpful in our quest to rationally design dominant negative leucine zipper domains which can sequester native c-Jun and c-Fos in neoplastic tissue (John et al., 1994).

### **ACKNOWLEDGMENT**

Dr. Bill Bubb is thanked for expert maintenance of the 600 MHz NMR spectrometer, and Dr. Peter Baron of Bruker Australia is thanked for providing time on their DRX500 NMR spectrometer. We thank Prof. Jean-François LeFèvre for valuable discussions and for raising the idea of using translational diffusion measurements to estimate rotational correlation times for the analysis of <sup>15</sup>N nuclear relaxation data. Dr. Bill Broadhurst and Dr. Martin Stone are thanked for valuable discussions. Andrew Dingley is thanked for assistance with the PFG NMR experiments.

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BI952761Y